

## College Algebra Formulas Tests – Use This to Study

Positive	Zero	Negative
$ 3x + 5  = 4$ <i>becomes</i> $3x + 5 = 4$ or $3x + 5 = -4$ (drop) (drop/sign flip)	$ 3x + 5  = 0$ <i>becomes</i> $3x + 5 = 0$	$ 3x + 5  = -4$ <i>has</i> No Solution

For inequalities involving absolute value:

...**positive**, rewrite as a compound or combined inequality without absolute value bars (see examples below)

> or ≥	$ 3x + 5  > 4$ <i>becomes</i> $3x + 5 > 4$ or $3x + 5 < -4$ (drop) (drop/double sign flip)	$ 3x + 5  ≥ 7$ <i>becomes</i> $3x + 5 ≥ 7$ or $3x + 5 ≤ -7$ (drop) (drop/double sign flip)
< or ≤	$ 3x + 5  < 9$ <i>becomes the combined inequality</i> $-9 < 3x + 5 < 9$	$ 3x + 5  ≤ 2$ <i>becomes the combined inequality</i> $-2 ≤ 3x + 5 ≤ 2$

...**zero**, rewrite as an equality or inequality, or state the solution as “All Real Numbers” or “No Solution” (see examples below)

> or ≥	$ 3x + 5  > 0$ <i>becomes the inequality</i> $3x + 5 ≠ 0$	$ 3x + 5  ≥ 0$ <i>has the solution</i> All Real Numbers
< or ≤	$ 3x + 5  < 0$ <i>has</i> No Solution	$ 3x + 5  ≤ 0$ <i>becomes the equality</i> $3x + 5 = 0$

...**negative**, state the solution as “All Real Numbers” or “No Solution” (see examples below)

> or ≥	$ 3x + 5  > -4$ <i>has the solution</i> All Real Numbers	$ 3x + 5  ≥ -7$ <i>has the solution</i> All Real Numbers
< or ≤	$ 3x + 5  < -9$ <i>has</i> No Solution	$ 3x + 5  ≤ -2$ <i>has</i> No Solution

Some equation forms of a line:

Slope-Intercept Form

$$y = mx + b$$

Point-Slope Form

$$y - y_1 = m(x - x_1)$$

Standard/General Form

$$Ax + By = C$$

Some equation forms of a circle:

Standard Form

$$(x - h)^2 + (y - k)^2 = r^2$$

General Form

$$x^2 + y^2 + ax + by + c = 0$$

The average rate of change of a function from  $a$  to  $b$  is  $\frac{f(b)-f(a)}{b-a}$

Given a line passing through points  $(x_1, y_1)$  and  $(x_2, y_2)$ , the slope  $m$  of the line is  $m = \frac{\text{rise}}{\text{run}} = \frac{y_2 - y_1}{x_2 - x_1}$   
as long as  $x_2 \neq x_1$

Some equation forms of a parabola:

Vertex Form

$$y = a(x - h)^2 + k$$

Standard Form

$$y = ax^2 + bx + c \text{ with vertex } \left(-\frac{b}{2a}, c - \frac{b^2}{4a}\right)$$

The Law of Exponents:

Given  $a > 0$  with  $a \neq 1$ : If  $a^u = a^v$  then  $u = v$

## SUMMARY Properties of Logarithms

In the list that follows,  $a, b, M, N$ , and  $r$  are real numbers. Also,  $a > 0, a \neq 1, b > 0, b \neq 1, M > 0$ , and  $N > 0$ .

**Definition** →

$$y = \log_a x \text{ means } x = a^y$$

**Properties of logarithms**

$$\log_a 1 = 0 \quad \log_a a = 1$$

$$a^{\log_a M} = M \quad \log_a a^r = r$$

$$\log_a(MN) = \log_a M + \log_a N$$

$$\log_a\left(\frac{M}{N}\right) = \log_a M - \log_a N$$

$$\log_a M^r = r \log_a M$$

$$a^x = e^{x \ln a}$$

$$\text{If } M = N, \text{ then } \log_a M = \log_a N.$$

$$\text{If } \log_a M = \log_a N, \text{ then } M = N$$

**Change-of-Base Formula** →

$$\log_a M = \frac{\log_b M}{\log_b a}$$

The compound interest formula states that  $F = P \left(1 + \frac{r}{n}\right)^{nt}$

The continuously compounded interest formula states that  $F = Pe^{rt}$

The exponential law states that an amount  $A$  varies with time  $t$  according to the function  $A(t) = A_0 e^{kt}$   
As long as the start time is 0, the value of  $k$  can be determined using the adder  $a$  and either the multiplier  $m$  or the divider  $d$ :

$$k = \frac{\ln m}{a} \quad \text{or} \quad k = \frac{\ln(1/d)}{a}$$